

**Title:** Galois representations with open image

**Abstract:** Suppose that  $p$  is a prime and that  $n \geq 1$ . Let  $G_{\mathbf{Q}} = \text{Gal}(\overline{\mathbf{Q}}/\mathbf{Q})$  be the absolute Galois group of  $\mathbf{Q}$ . Let  $\mathbf{Z}_p$  denote the ring of  $p$ -adic integers. Our purpose in this talk is to describe a way of constructing continuous representations

$$\rho : G_{\mathbf{Q}} \longrightarrow GL_n(\mathbf{Z}_p)$$

whose image is open. This means that the image of  $\rho$  has finite index in  $GL_n(\mathbf{Z}_p)$ . We can do this for many pairs  $(n, p)$ . One typical result is the following:

**Proposition:** *Suppose that  $p$  is a regular prime and that  $p \geq 4\left[\frac{n}{2}\right] + 1$ . Then there exists a continuous representation  $\rho$  as above with open image.*