Exercise Set 5:

Public-key Cryptography – Diffie-Hellman and RSA

Math 414, Winter 2010, University of Washington

Due Friday, February 12, 2010

- 1. You and Nikita wish to agree on a secret key using the Diffie-Hellman key exchange. Nikita announces that p = 3793 and g = 7. Nikita secretly chooses a number n < p and tells you that $g^n \equiv 454 \pmod{p}$. You choose the random number m = 1208. What is the secret key?
- 2. You see Michael and Nikita agree on a secret key using the Diffie-Hellman key exchange. Michael and Nikita choose p = 97 and g = 5. Nikita chooses a random number n and tells Michael that $g^n \equiv 3$ (mod 97), and Michael chooses a random number m and tells Nikita that $g^m \equiv 7 \pmod{97}$. Brute force crack their code: What is the secret key that Nikita and Michael agree upon? What is n? What is m?
- 3. In this problem, you will "crack" an RSA cryptosystem. What is the secret decoding number d for the RSA cryptosystem with public key (n, e) = (5352381469067, 4240501142039)?
- 4. Nikita creates an RSA cryptosystem with public key

(n, e) = (1433811615146881, 329222149569169).

In the following two problems, show the steps you take to factor n. (Don't simply factor n directly using a computer.)

- (a) Somehow you discover that d = 116439879930113. Show how to use the probabilistic algorithm in the book to factor n.
- (b) In part (a) you found that the factors p and q of n are very close. Show how to use the Fermat Factorization Method in the book to factor n.